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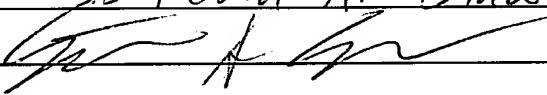
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METHOD FOR TRIANGLE SUBDIVISION  
IN COMPUTER GRAPHICS TEXTURE MAPPING  
TO ELIMINATE ARTIFACTS IN HIGH PERSPECTIVE POLYGONS

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METHOD FOR TRIANGLE SUBDIVISION  
IN COMPUTER GRAPHICS TEXTURE MAPPING  
TO ELIMINATE ARTIFACTS IN HIGH PERSPECTIVE POLYGONS

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### FIELD OF THE INVENTION

The present invention relates to the field of graphics imaging and the display of images on a screen. More particularly, the present invention relates to a method for presenting computer generated objects on a two-dimensional graphics display with perspective texture mapping in a computer controlled graphics display system.

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### BACKGROUND OF THE INVENTION

It is becoming more common for workstations and general purpose computer systems to be used for visual simulations. Such simulations are 15 particularly useful in high end systems for industrial modeling applications and in lower end systems for entertainment (e.g., simulations, computer games, multi-media applications, etc.). Computer controlled graphics systems display graphics objects on a 2 dimensional (2-D) display; the graphics objects being composed of graphics primitive elements ("graphics primitives") that may include, for instance, points, lines, polygons, etc. 20 represented using three dimensional (3-D) data structures (e.g., x, y, z). As is well known, the object displayed is represented internally by the graphics system with three dimensional (3-D) data structures (e.g., x, y, z) which are transformed into 2-D elements (e.g., x, y) which are then used to render a 2-D 25 image of the 3-D object.

Texture mapping refers to techniques for adding surface detail to areas or surfaces of these 3-D graphics objects displayed on the 2-D display.

Since the original graphics object is 3-D, texture mapping often involves maintaining certain perspective attributes with respect to the surface detail

added to the object. Generally, texture mapping occurs by accessing encoded surface detail points or "texels" from a memory which stores the surface detail and then transferring the surface detail texels to predetermined points of the graphics primitive that is texture mapped. More specifically,

5 texture mapping operates by applying color or visual attributes of texels of the (u, v) texture map to corresponding pixels of the graphics object on a display screen. In texture mapping, color values for pixels in (x, y) display coordinate space are determined based on sampled texture map values from (u, v) coordinates. After texture mapping, a version of the texture image is visible

10 on surfaces of the object. The manner in which the texels are accessed and used to provide the perspective is a complex process that can utilize interpolation which increases processing speed but provides only an "estimation" of the true perspective condition.

There are three types of texture mapping including linear, second order homogeneous perspective and second order non-homogeneous perspective. In linear texture mapping, texels of a texture map are generally mapped onto pixels of a 2-D graphics primitive linearly whereby the rate of sampling in texel space (u, v) with respect to the screen coordinate (x, y) update rate is constant, e.g.,  $du/dx$  and  $du/dy$  are constant values. In

15 perspective texture mapping, texels of a texture map are generally mapped onto pixels of a 3-D graphics object that is displayed in 2-D space (x, y) wherein the rate of sampling in texel space with respect to the rate of screen coordinate update rate is not constant. Perspective texture mapping, as discussed above, therefore features an illusion of depth which is created by

20 varying the sampling rate of the texture map during the normal linearly performed polygon rendering process on the display screen.

In one system, a graphics subsystem (accelerator) performs the necessary processing to generate the simulation in real-time using interpolation driven processes to perform texture mapping. Typically, the

graphics subsystem includes local memory for storing graphics data in a "display list" and a graphics engine that determines the texture (e.g., texture mapping) to be applied to picture elements (pixels) to form the simulation on the computer systems graphics display. Using techniques that are well understood by those skilled in the art, display images are first decomposed into graphics primitives comprising multiple polygons each of which may be readily rotated or otherwise transposed by the graphics subsystem before being sent to the frame buffer memory. As the perspective of the viewer changes, the displayed images must be redrawn to provide the proper visual perspective. Accordingly, graphics engines must be capable of mapping the texture onto the polygons in real-time as the position of the polygons are rotated, translated or otherwise shifted.

Using techniques to provide correct perspective, the graphics engine maps the three dimensional coordinates (x, y, z) of the polygon to corresponding texture coordinates (u, v). Whenever a pixel in the projection of the image is about to be plotted on the display screen, an association is formed between the vertices of the polygon and the pixels of the image while the image is being rendered. Also associated with each vertex is a perspective value, W, that defines the spatial relation of objects with respect to their relative distance and position as they might appear to the eye of a viewer when rendered on the display.

In low cost graphic engines interpolation driven texture mapping and rendering processes are used to speed the rendering process and limit memory requirements. However, maintaining proper orientation of the texture map with respect to the polygon as the perspective changes and interpolating interior (u, v) texels requires extensive computing power to prevent distortion, artifacts, wavy appearances, aliasing or other rendering errors. For images such as would be displayed in a video game with, by way of example, a road disappearing into the distance at infinity (Figure 2), the

perspective can vary from  $W=1$  for objects near the front of the screen perceived as close to the viewer to  $W=6$  or  $W=10$  (or greater) for objects receding into the distance near the back of the screen. Massive perspective (e.g.,  $W>5$ ) in real-time computer simulations often cause hardware

5 rendering engines to break down creating readily visible artifacts in the image when displayed. In one system, it has been determined that the breakdown point commonly occurs whenever a perspective ratio varies by more than about 1.5. It would be advantageous to provide a system that performs real-time simulation that avoids artifacts when processing images  
10 with massive perspective. It would be further advantageous to provide such a system that operates in conjunction with an interpolation driven texture mapping and rendering system. The present invention provides this  
advantageous capability

A further problem often encountered in rendering graphic images  
15 arises when two polygons share a common or co-linear edge. Depending on the manner in which the graphics subsystem interprets the image, however, the resulting object as rendered on the display will often have missing pixels or gaps along the common edge. Such gaps occur when the process employed by the graphics subsystem is not able to walk to common  
20 endpoints. Accordingly, it is desirable to draw polygons having a co-linear edge without tearing or creation of false edges or gaps. The present invention provides this advantageous capability.

#### SUMMARY OF THE INVENTION

25 The present invention relates to rendering three-dimensional graphics images on a computer controlled display system and more particularly to a system and method that eliminates artifacts created when large polygons with high perspective ratios are rendered/ texture mapped. The present invention is particularly useful within a computer controlled display system

utilizing interpolation driven rendering/texture mapping processes. The system and method of the present invention performs an iterative operation that subdivides selected polygons into a plurality of smaller polygons to limit artifact creation during the interpolation driven rendering/texture mapping processes.

Specifically, the processing logic of the present invention analyzes each polygon stored in display list memory of a graphics accelerator or graphics subsystem and determines a perspective ratio between adjacent vertices of the polygon. If the perspective ratio is greater than a pre-selected limit, the edge bounded by the vertices is subdivided at the mid-point and new triangles created. The process is iterative until all polygons have perspective ratios that are less than the pre-selected limit at which time the object data can be rasterized and displayed by the hardware.

Since the subdivision is based on determining the midpoint of edges rather than vertices of the polygon, any original polygon that shares the selected edge (and there might be several) will share a common vertex because the edge will be subdivided at the same mid-point thereby limiting creation of artifacts even if the edge appears later in the data stream.

Further, since the processing logic of the present invention consistently subdivides the edge each time it is encountered, objects are consistently rendered regardless of the coordinates of the vertices of the various polygons sharing the edge or having a co-incident edge.

The present invention calculates perspective values (w) and new coordinates (x, y, z) for each mid-point based on a simple average of the perspective values at the vertices bounding the edge. Texture coordinates at the mid-point of a divided edge (umid, vmid) are calculated by the processing logic and are interpolated across the polygon to determine the texel value of the image at each pixel within the boundary of the polygon.

## BRIEF DESCRIPTION OF THE DRAWINGS

Figure 1 illustrates a computer controlled graphics display system having a host processor and a graphics subsystem with the capability of rendering visual simulations on a display screen.

5 Figure 2 is an illustrative representation of a displayed image with perspective within a visual simulation.

Figure 3 is a representation of two polygons within a displayed image having perspective within a visual simulation.

10 Figures 4A and 4B illustrate a flow diagram of processing logic in accordance with the present invention that is implemented on the computer controlled display system shown in Figure 1 that divides polygons when one or more perspective ratios exceed a selected threshold before the polygons are rendered on the display system.

15 Figures 5A and Figure 5B illustrate, respectively, a perspective view of a polygon having perspective ratios exceeding the preselected limit and a perspective view of the polygon after being split in accordance with the present invention.

20 Figures 5C and Figure 5D illustrate, respectively, a perspective view of a polygon having a perspective ratio exceeding the preselected limit and a perspective view of the polygon after being split in accordance with the present invention.

25 Figure 6A and Figure 6B illustrate a flow diagram of processing logic for determining new 3-D coordinates (x, y, z), perspective terms (W), texture coordinates (u, v), and color values (R, G, B) for midpoints determined in accordance with the present invention.

Figures 7A, 7B, and 7C illustrate three possible triangle split configurations when one of the three triangle edges exceeds the perspective ratio in accordance with the present invention.

Figures 8A, 8B, and 8C illustrate three possible triangle split configurations when two of the three triangle edges exceed the perspective ratio in accordance with the present invention.

Figure 9 illustrates one triangle split configuration when all of the 5 three triangle edges exceed the perspective ratio in accordance with the present invention.

#### DESCRIPTION OF THE PREFERRED EMBODIMENTS

In the following description of the preferred embodiment, reference is 10 made to the accompanying drawings which form a part hereof, and in which is shown by way of illustration a specific embodiment in which the invention may be practiced. It is to be understood that other embodiments may be utilized and that changes may be made without departing from the scope of the present invention. For purposes of illustration the following description 15 describes the present invention as used with a computer system equipped to display graphics in real-time. However, it is contemplated that the present invention can be used in conjunction with other digital display systems.

Reference will now be made in detail to the preferred embodiments of the invention, examples of which are illustrated in the accompanying drawings. 20 Wherever possible, the same reference numbers will be used throughout in the drawings to refer to the same or like components.

#### NOTATION AND NOMENCLATURE

Some portions of the detailed descriptions which follow are presented 25 in terms of procedures, logic blocks, processing, and other symbolic representations of operations on data bits within a computer or digital system memory. These descriptions and representations are the means used by those skilled in the data processing arts to most effectively convey the substance of their work to others skilled in the art. A procedure, logic block,

process, etc., is herein, and generally, conceived to be a self-consistent sequence of steps or instructions leading to a desired result. The steps are those requiring physical manipulations of physical quantities. Usually, though not necessarily, these physical manipulations take the form of

5 electrical or magnetic signals capable of being stored, transferred, combined, compared, and otherwise manipulated in a computer system. For reasons of convenience, and with reference to common usage, these signals are referred to as bits, values, elements, symbols, characters, terms, numbers, or the like with reference to the present invention.

10 It should be borne in mind, however, that all of these terms are to be interpreted as referencing physical manipulations and quantities and are merely convenient labels and are to be interpreted further in view of terms commonly used in the art. Unless specifically stated otherwise as apparent from the following discussions, it is understood that throughout discussions of

15 the present invention, discussions utilizing terms such as "processing" or "computing" or "calculating" or "determining" or "displaying" or the like, refer to the action and processes of a computer system, or similar electronic computing device, that manipulates and transforms data. The data is represented as physical (electronic) quantities within the computer system's registers and memories and is transformed into other data similarly represented as physical quantities within the computer system memories or registers or other such information storage, transmission or display devices.

#### COMPUTER SYSTEM PLATFORM

25 Refer to Figure 1 which illustrates a computer controlled display system ("computer system") 112. Within the following discussions of the present invention, certain processes (e.g., processes 400, 485, and 610) are discussed that are realized, in one implementation, as a series of instructions (e.g., software program) that reside within computer readable memory units of

system 112 and executed by processors of system 112. When executed, the instructions cause the computer system 112 to perform specific actions and exhibit specific behavior which is described in detail to follow.

- In general, computer system 112 used by the present invention
- 5 comprises an address/data bus 100 for communicating information, one or more central processors 101 coupled with the bus 100 for processing information and instructions, a computer readable volatile memory unit 102 (e.g., random access memory, static RAM, dynamic, RAM, etc.) coupled with the bus 100 for storing information and instructions for the central
  - 10 processor(s) 101, a computer readable non-volatile memory unit (e.g., read only memory, programmable ROM, flash memory, EPROM, EEPROM, etc.) coupled with the bus 100 for storing static information and instructions for the processor(s) 101. As will be appreciated by person of ordinary skill in the art, memory 104 may contain information, such as application programs, network
  - 15 communication programs, operating systems, data, graphics display data etc.

System 112 also includes a mass storage computer readable data storage device 104 (hard drive or floppy) such as a magnetic or optical disk and disk drive coupled with the bus 100 for storing information and instructions. Optionally, system 112 can include a display device 105 for displaying information to the computer user, an optional alphanumeric input device 106 including alphanumeric and function keys coupled to the bus 100 for communicating information and command selections to the central processor(s) 101, an optional cursor control device 107 coupled to the bus for communicating user input information and command selections to the central processor(s) 101, and an optional signal generating device 108 coupled to the bus 100 for communicating command selections to the processor(s) 101. In one exemplary implementation, system 112 is an x86 microprocessor based computer system, but could equally be of a number of other various

well known and commercially available platforms (e.g., DEC Alpha, Power PC, RISC based, etc.).

The host processor 101 provides data and control signals via bus 100 to a graphics subsystem 109. The graphics subsystem 109 typically 5 contains a display processor 109a which executes/processes a series of display instructions and graphics primitives found within a display list stored in local volatile memory 109b. The display processor 109a supplies data and control signals to a frame buffer (not shown) which refreshes the display device 105 for rendering images (including graphics images). Specialized 10 and well known circuits 109c are also included in graphics subsystem 109 for implementing sound and graphics special effects and perform high speed graphics processing. Although not shown, the graphics subsystem 109 can be directly coupled to drive display device 105. Graphics subsystem 109 also typically is granted high priority access to memory 104 for processing 15 image data prior to display.

To display a three-dimensional (3-D) object on display 105, the object is decomposed by system 112 into a plurality of graphics commands and graphic primitives including, for example, polygons (e.g., triangles), lines and points to obtain a representation of the object. In one embodiment, polygons 20 are triangles having three vertices, but could also include geometric representations having more than three vertices (e.g., rectangles, etc.). As used herein, the term polygon and triangles are used interchangeably unless specifically otherwise noted. The vertices of the triangles are described by respective three dimensional Cartesian coordinates (x, y, z). 25 The vertices are stored in either memory 104 or in the local memory 109b of graphics subsystem 112 and define the object's shape and position.

System 112 applies texture maps to the displayed surfaces of the graphics triangles to provide surface shading, volume rendering or to otherwise present a realistic appearance of the object. A texture is image

data ("texels") that are mapped or matched to the pixels of the polygons of the graphics primitives so that the displayed object has the appearance of realism. Graphic subsystem 109 maps texture by matching texture coordinates (u, v) with a corresponding vertex of the polygon and then

5 rendering the image on the display screen. In one embodiment, texture inside the polygon is determined by interpolation within subsystem 109; one process of which is described in more detail in copending patent application entitled Non-Homogenous Second Order Perspective Texture Mapping Using Linear Interpolation Parameters, by Gautam P. Vaswani et al., filed on  
10 December 30, 1996, serial number 08/403,460, and assigned to the assignee of the present invention. In general, the basic steps of the texture mapping process are to: assign texture coordinates to the vertices of each polygon to define a mapping function from texture coordinate space to the display coordinates in display space; interpolate to determine corresponding  
15 texture coordinates for each pixel coordinate within the polygon based on the texture coordinates assigned to the polygon's vertices and based on certain parameters computed for the polygon; and assign textual values to each pixel inside the polygon during the rendering process based on the determined texel coordinates.

20

#### GENERAL OPERATION OF PRESENT INVENTION

Referring now to Figure 2, the present invention is illustrated by way of example using an airport runway 202 as the object to be rendered on display 105. Runway 202 is shown composed of two polygons, one polygon  
25 having vertices A, B, D and the other polygon having vertices B, D, C.

Texture mapping provides the appearance of asphalt or concrete to runway 202 and applies a centerline 204, and end-of-runway stripes 206. The position of each vertex on the display screen is determined based on a viewing angle and based on the set of Cartesian coordinates (x, y, z) for

each vertex (A, B, C, D). Also associated with each of the vertices are well known perspective terms,  $WA$ ,  $WB$ ,  $WC$  and  $WD$ , respectively for vertex A, B, C, and D. In general, when  $WA = WB = WC = WD = 1$ , the polygon lies in the XY-plane with  $z = 0$  for each vertex and when  $WA = WB = WC = WD$  the

5 corresponding vertices lie in a single XY-plane with a common Z coordinate for each vertex.

To maintain visual perspective as runway 202 is rotated with respect to a common viewing angle, the perspective terms ( $W$ ) of the vertices change depending on the point of view of the observer. The perspective can vary

10 from  $W=1$  for objects near the front of the screen 105 which are perceived as close to the viewer, to  $W=6$  or  $W=10$  for objects receding into the distance near the back of the screen. Such large perspective (e.g.,  $W>6$ ) in real-time computer simulations often cause hardware rendering engines to break down creating readily visible artifacts. This is particularly true when linear

15 interpolation rendering/texture mapping processes of subsystem 109 are used which perform estimations to determine the proper texture map values.

It has been determined that with respect to the above cited linear

interpolation process, the breakdown point begins to occur when the ratio of the perspective terms amount to 1.5 or more for any given triangle edge (an

20 edge having a vertex pair from which the ration is determined).

Therefore, the present invention determines if the amount of perspective in a displayed image will create visible artifacts or distortion during the rendering process, and if so, the triangle is divided, and subdivided if need be, until it is determined that visible artifacts are removed.

25 The operation of the present invention is first described generally, and then described in detail with respect to Figure 4A and Figure 4B.

Simultaneously with, or prior to, building a display list in local memory 109b, the present invention calculates and compares perspective ratios of each triangle to be displayed. Specifically, the perspective ratios of each

vertex pair for each triangle edge are calculated. For instance, the ratios:

WA/WB, WB/WA, WB/WD, WD/WB, WD/WA, WA/WD are calculated for triangle ABD of Figure 2 and WB/WC, WC/WB, WB/WD, WD/WB, WD/WC, WC/WD are calculated for triangle BDC of Figure 2. If any of the above

5 perspective ratios exceed a selected ratio threshold, the edge between the selected vertices is split (thus forming new triangles) by system 112 to prevent the creation of artifacts during the rendering process.

In accordance with the present invention, processing logic resident in either memory 104 (Figure 1) or the local memory 109b of graphics

10 subsystem 109 (or memory 103), compares each ratio to the given threshold and, in the event one or more edge pairs violate the threshold, subdivides the edge between the vertices corresponding to the perspective ratio and finds the mid-point of the edge. Splitting edges causes new triangles to be formed. If only one edge is split, two triangles result from one original  
15 triangle. If two edges need to be split in the original triangle, then three triangles result. If all three edges need to be split in the original triangle, then four triangles result. Edges are split via their mid-point. The midpoint is determined, in one preferred embodiment, by adding together the corresponding coordinates of the vertices of the edge using fixed point math  
20 and shifting the sum to affect a divide by two operation and a new vertex is assigned to the mid-point.

As described above, depending on the number of edges split, new triangles are created by connecting vertices and/or midpoints of the original triangle. The processing logic of the present invention then calculates new  
25 coordinates (x, y, z), new perspective terms (W), new texture coordinate values (u, v), and new color values (R, G, B), Red, Green, Blue, for any midpoints created. In one embodiment, a perspective term, WMid, is computed using a simple average of the perspective values at each of the vertices bounding the edge segment that has been divided. Accordingly, the

perspective term, WMid, is assigned to the mid-point vertex and stored in memory 104 or memory 109b. It is appreciated that if any edge of the newly created triangles violates the threshold perspective ratio, that violating triangle is similarly split as described above, and so forth until all triangles of 5 a particular display meet the perspective threshold.

In Figure 3, exemplary runway 202 is illustrated superimposed on the 3-D coordinate system (x, y, z) without texture data. As shown, the runway polygon can be represented by two triangles ABD and BCD having a common edge BD. Advantageously, if only one edge violates the threshold 10 perspective ratio, the processing logic of the present invention only subdivides triangles sharing that edge. However, if  $WD = 10$  and  $WA = WB = 1$ , edges AB and BD will be divided in accordance with the below described process. After the processing logic has created a plurality of triangles each having perspective ratios of, in the preferred embodiment, between 1.25 and 15 1.5 (e.g., 1.45), or less, the resultant triangles are stored into a display list within local memory 109b to be further processed by graphics subsystem 109 and rendered on display 105.

Since divisions in accordance with the present invention are based on the edge rather than one or more vertices of the triangle, any original 20 triangle that shares the selected edge, (and there might be several), will share the common mid-point vertex because the edge will be broken in the exact same manner thereby limiting artifacts even if you see the edge again with respect to another triangle much later in the display data stream. Since the process of the present invention consistently breaks up the edge each 25 time it is encountered, the effect is to consistently rendering of the edge regardless of the coordinates of the vertices of the various triangles sharing the edge.

## FLOWCHART OPERATION OF PRESENT INVENTION

Figure 4A and Figure 4B illustrate a flow diagram of steps of process 400 executed by the present invention. It is appreciated that the processing logic 400 can be embedded in a pre-processor (e.g., hardcoded in memory

- 5 103 or another non-volatile memory unit of subsystem 109), performed by the host processor 101, or alternatively implemented as an application software module performed by graphics subsystem 109. In any event, process 400 is realized as software or instruction code stored in computer readable memory units of system 112. Processing logic 400 begins
- 10 execution at an initialization step 410 (Figure 4A) which includes selecting or receiving a maximum perspective ratio ("perspective threshold"), W\_Ratio\_Threshold, which in the preferred embodiment is 1.45 but can be varied. It is appreciated that the maximum perspective ratio, in one embodiment, is determined based on a user selected value from a
- 15 performance/quality knob which is a user selectable knob that trades off speed of performance (e.g., rendering) versus image quality; in this embodiment the maximum perspective ratio can and is expected to change depending on user performance/quality determinations.

- At step 415, a polygon 310 (Figure 5A) is selected (e.g., the selected polygon) from the display data list stored in local memory 109b of graphics subsystem 109. Alternatively, polygon 310 can be supplied from host processor 101 over bus 100. Polygon 310, as shown in Figure 5A, includes vertices ABD. At step 420, the coordinates (x, y, z) of the vertices of the polygon of Figure 5A are retrieved, the perspective terms WA, WB, and WD for vertices A, B, and D, respectively, are retrieved, and the RGB values and the texture coordinates (u, v) for each vertex of polygon 310 are retrieved.

Processing step 430 of Figure 4A then calculates perspective ratios between each of the three edges of polygon ABD. Specifically, with respect to triangle ABD, perspective ratios are calculated for vertices pairs (edges): A

and B; B and D; and A and D. The following perspective ratios are computed for each selected polygon at step 430:

5            Perspective Ratio1 = WA/WB  
              Perspective Ratio2 = WB/WA  
              Perspective Ratio3 = WB/WD  
              Perspective Ratio4 = WD/WB  
              Perspective Ratio5 = WA/WD  
              Perspective Ratio6 = WD/WA

10

At step 440 of Figure 4A, it is determined whether or not the computed perspective ratios of at least three different edges violate (e.g., exceed) the maximum perspective threshold amount, W\_Ratio\_Threshold. If so, step 480 (Figure 4B) is entered. If not, then at step 450, it is determined whether or 15 not the computed perspective ratios of two different edges violate (e.g., exceed) the maximum perspective threshold amount, W\_Ratio\_Threshold, and that three different edges do not violate. If so, step 475 (Figure 4B) is entered. If not, then at step 460, it is determined whether or not the computed perspective ratios of one edge violates (e.g., exceed) the 20 maximum perspective threshold amount, W\_Ratio\_Threshold, and that two nor three edges violate. If so, step 470 (Figure 4B) is entered. If not, then step 500 (Figure 4B) is entered.

At step 440 of Figure 4A, if three different edges of polygon 310 violate, then processing flows to step 480 of Figure 4B where, as shown in 25 Figure 9, midpoints 12, 20 and 30 are determined and the selected polygon ABD 310 is divided with four new triangles 72, 74, 76, and 78 being generated. Triangle 72 is made up of vertex A, midpoint 12 and midpoint 30; triangle 74 is made up of vertex D, midpoint 20 and midpoint 30; triangle 76 is made up of vertex B, midpoint 20 and midpoint 12; and triangle 78 is made 30 up of midpoints 12, 20 and 30. Then step 485 is entered.

In one particular embodiment of the present invention, the above perspective ratios can be computed by step 430 and then can be compared by step 440 (e.g., for

triangle ABD) without using a divide operation according to the pseudo code format below:

5      vertex1.w = WA  
vertex2.w = WB  
vertex3.w = WD  
max\_w\_ratio = W\_Ratio\_Threshold  
w1\_times\_max = vertex1.w \* max\_w\_ratio  
w2\_times\_max = vertex2.w \* max\_w\_ratio  
w3\_times\_max = vertex3.w \* max\_w\_ratio  
if      ( (vertex1.w < w2\_times\_max) AND (vertex1.w < w3\_times\_max) AND  
          (vertex2.w < w1\_times\_max) AND (vertex2.w < w3\_times\_max) AND  
          (vertex3.w < w1\_times\_max) AND (vertex3.w < w2\_times\_max) )  
then no perspective violation  
15     else perspective violation

At step 450 of Figure 4A, if two different edges of the selected polygon 310 violate, and three edges do not, then processing flows to step 475 of Figure 4B where the present invention divides the selected polygon 310 into three triangles, depending on which two edges violate. As shown in Figure 8A, if the edge between vertex A and vertex B violates and the edge between vertex B and vertex D violates, then at step 475, polygon 310 is divided into triangles 42, 44, and 46, with triangle 42 made up of vertex B, midpoint 12 and midpoint 20; triangle 44 made up of vertices A and D and midpoint 20; and triangle 46 made up of midpoints 12, 20 and vertex A. As shown in Figure 8B, if the edge between vertex B and vertex D violates and the edge between vertex D and vertex A violates, then at step 475, polygon 310 is divided into triangles 52, 54, and 56, with triangle 52 made up of vertices A, B, and midpoint 30; triangle 54 made up of midpoints 20, 30 and vertex B; and triangle 56 made up of midpoints 20, 30 and vertex D. As shown in Figure 8C, if the edge between vertex D and vertex A violates and the edge between vertex A and vertex B violates, then at step 475, polygon 310 is divided into triangles 62, 64, and 66, with triangle 62 made up of midpoints 12, 30 and vertex A; triangle 64 made up of midpoints 12, 30 and

vertex B; and triangle 66 made up of vertices B, D and midpoint 30. Then step 485 is entered.

At step 450 of Figure 4A, if one different edge violates and three edges and two edges do not, then processing flows to step 470 of Figure 4B

5 where the present invention divides the selected polygon 310 into two triangles, depending on which edge violates. As shown in Figure 7A, if the edge between vertex A and vertex B violates, then at step 470, polygon 310 is divided into triangles 14 and 18, with triangle 14 made up of vertices A, D and midpoint 12; and triangle 18 made up of vertices B, D and midpoint 12.

10 As shown in Figure 7B, if the edge between vertex B and vertex D violates, then at step 470, polygon 310 is divided into triangles 22 and 24, with triangle 22 made up of vertices A, D and midpoint 20; and triangle 24 made up of vertices A, B and midpoint 20. As shown in Figure 7C, if the edge between vertex A and vertex D violates, then at step 470, polygon 310 is

15 divided into triangles 32 and 34, with triangle 32 made up of vertices B, D and midpoint 30; and triangle 34 made up of vertices A, B and midpoint 30.

Then step 485 is entered.

At step 485 of Figure 4B, the three dimensional coordinates (x, y, z), the colors (R, G, B), the texture coordinates (u, v) and the perspective term, 20 (W, are computed for any midpoints (e.g., 12, 20, and 30) created by steps 470, 475, and 480. The manner in which these computations are performed is described in further detail with respect to Figure 6A and Figure 6B.

At step 490 of Figure 4B, the selected polygon 310 is replaced by all new triangles generated by steps 470, 475 and 480. In particular, the 25 selected polygon 310 (within the display list) is replaced by all newly generated triangles of steps 470, 475 and 480 with the newly generated triangles marked as "unselected" as stored in the display list. The new triangles are marked as unselected so that they can each be separately sent through process 400 and tested for perspective violations themselves. At

step 495, a pointer is updated so that a new unselected polygon is selected as the selected polygon 310. Processing then returns to step 414 of Figure 4A.

At step 500 of Figure 4B, system 112 checks if the selected polygon 310 is the last polygon of the display list and there are no more "unselected" polygons in the display list. If so, process 400 completes and all triangles in the display list now satisfy the maximum perspective threshold. If not, then step 495 is entered to select a new polygon for processing. Upon each polygon being processed, the display list in 109b is then rendered for display. In one embodiment of the present invention, the interpolation driven rendering/texture map process cited above is used to perform texture mapping and image rendering onto display 105 (Figure 1).

It is appreciated that process 400 of Figure 4A and Figure 4B is described with respect to a system that checks all polygons in the display list before rendering. However, process 400 is equally well suited for application within system that processes polygons 310 iteratively for display. For example, a system that decomposes a single polygon (from the display list) into its sub-triangles, stores the subtriangles into memory, divides any subtriangles if needed, then when all subtriangles meet the perspective threshold, renders all sub-triangles on display 105 and then accesses the next polygon of the display list.

#### EXAMPLES:

As an example of the operation of process 400, Figure 5A illustrates perspective terms arbitrarily assigned for each vertex of polygon 310, with WA=1.0, WB=1.0 and WD=1.8. In ratio determining step 430, the ratio WD/WB is determined to be 1.8 (exceeding threshold of 1.45 as set by W\_Ratio\_Threshold) and this edge (BD) is determined to exceed the threshold. Further, the ratio WD/WA is also determined to be 1.8, so edge

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(DA) also exceeds the threshold. Accordingly, two edges violate, so step 450 responds in the affirmative. Polygon 310 is then split in accordance with Figure 8B into triangles 52, 54, and 56 as shown in Figure 5B. The newly generated triangles 52, 54, and 56 will be resubmitted to process 400 to 5 determine whether the new perspective ratios exceed the limit set by W\_Ratio\_Threshold in accordance with the present invention.

As another example, Figure 5C illustrates that perspective terms for each vertex have been arbitrarily assigned to polygon 310 with WA=1.4, WB=1.0 and WD=1.8. In ratio determining step 430, the ratio WD/WB is 10 determined to be 1.8 (exceeding threshold of 1.45 as set by W\_Ratio\_Threshold) and this edge is determined to exceed the threshold. However, the other edges do not violate the perspective threshold. Accordingly, one edge violates, so step 460 responds in the affirmative. Polygon 310 is then split in accordance with Figure 7B into triangles 22, and 15 24 as shown in Figure 5D. The newly generated triangles 22 and 24 will be resubmitted to process 400 to determine whether the new perspective ratios exceed the limit set by W\_Ratio\_Threshold.

Once all perspective ratios of all edges of all polygons of the display list are less than the selected perspective threshold, the procedure of Figure 20 4 is terminated and the graphics data may be rendered to the display screen 105 without noticeable artifacts. To avoid creating tearing or creation of artifacts when two triangles, such as triangle ABD and BCD, share a common co-linear edge (such as, for example, edge BD), the present invention consistently splits edges in the same location. It is an advantage of 25 the present invention that inserted vertices will always be at the identical coordinate on common edges regardless of whether triangle ABD or BCD is processed for display and without regard to relative positioning of the triangles in the display stream. Accordingly, the object is rendered without missing pixels or gaps along common or co-linear edges.

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For image rendition requiring high image quality, the W\_Ratio\_Threshold can be selected so that each triangle is divided into a higher number of triangles in order to achieve the desired image quality. For example, W\_Ratio\_Threshold may be selected from the range of 1.2 to a 5 maximum value where such maximum value is a function of graphics subsystem 109. Alternatively, if high image quality is not required or desired due to memory or speed constraints, the variable, W\_Ratio\_Threshold, may be selected from the range of 1.5 to about 3 or 5. The actual range may be selected based on the type of images being rendered and the viewer's 10 balance of performance over quality.

#### STEP 485 OF PROCESS 400

As discussed above, at step 485 of Figure 4B, the three dimensional coordinates (x, y, z), the colors (R, G, B), the texture coordinates (u, v) and 15 the perspective value, W, are computed for all midpoints 12, 20, and 30. Figures 6A and Figure 6A illustrate a flow chart of the steps performed by process 485 used to determine these values in accordance with the present invention. At step 610 of Figure 6A, the new values for (R, G, B), (x, y, z) and W are computed for each new midpoint generated by process 400. The 20 following relationships are used assuming an edge comprising vertex A and vertex B is divided and assuming further vertex A has coordinates (xA, yA, zA) and vertex B has coordinates (xB, yB, zB). Further, vertex A has perspective term, WA, and colors (RA, GA and BA) and vertex B has perspective term, WB, and colors (RB, GB and BB). Step 600 is performed 25 using the following relationships:

$$W_{midpoint} = (WA + WB) / 2$$

$$R_{midpoint} = (RA + RB) / 2$$

$$G_{midpoint} = (GA + GB) / 2$$

$$B_{midpoint} = (BA + BB) / 2$$

$$x_{midpoint} = (xA + xB) / 2$$

$$y_{midpoint} = (yA + yB) / 2$$

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$$z_{\text{midpoint}} = (z_A + z_B) / 2$$

where  $(x_{\text{midpoint}}, y_{\text{midpoint}}, z_{\text{midpoint}})$  are the  $(x, y, z)$  coordinates of the new midpoint of the divided edge  $(AB)$ ,  $(R_{\text{midpoint}}, G_{\text{midpoint}}, B_{\text{midpoint}})$

5 are the  $(R, G, B)$  color values of the new midpoint, and  $W_{\text{midpoint}}$  is the perspective term of the new midpoint of the divided edge.

Values for texture coordinates  $(u, v)$  at the midpoint of the divided edge, that is  $(u_{\text{mid}}, v_{\text{mid}})$ , are calculated by step 610 of Figure 6A which is described in more detail in the processing logic shown in Figure 6B. At

10 processing step 615 the texture coordinates,  $(u_A, v_A)$  and  $(u_B, v_B)$ , and perspective terms,  $W_A$  and  $W_B$ , for each vertex (e.g., vertex A and vertex B) bounding a divided edge are obtained. At process step 620, intermediate variables,  $a$  and  $b$ , are calculated according to the following relationships:

15  $a = u_A * W_A$

where  $u_A$  denotes the  $u$ -axis texture coordinate at vertex A while  $W_A$  denotes the perspective value at vertex A;

and

20

$$b = u_B * W_B$$

where  $u_B$  denotes the  $u$ -axis texture coordinate at vertex B while  $W_B$  denotes the perspective value at vertex B. Intermediate variable,  $c$ , is then

25 calculated at process step 625 of Figure 6B according to the relationship below:

$$c = (a+b) / 2$$

30 and  $u_{\text{mid}}$  is then calculated at process step 630 according to:

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$$umid = c / Wmid$$

As shown in processing steps 635-650, a value for vmid is calculated  
5 in accordance with the process logic in steps 620-630 by replacing u-axis  
texture coordinates, uA and uB, with the corresponding v-axis texture  
coordinates, vA and vB for vertices A and B. At the completion of step 650,  
the texture coordinates (umid, vmid) are computed. With the newly  
determined texture coordinates, texture data can be interpolated for pixels  
10 within each triangle based on the (u, v) coordinates assigned to the vertices  
of the triangle.

In one embodiment, the present invention does not require  
substantial, if any, modification to be made to hardware graphics subsystems  
previously installed in computer system 112. Although described with  
15 respect to an interpolation driven texture mapping/rendering system, the  
present invention polygon split procedure can operate in conjunction with  
any hardware subsystem that performs 3-D texture mapping operations.

While certain exemplary preferred embodiments have been described  
and shown in the accompanying drawings, it is to be understood that such  
20 embodiments are merely illustrative of and not restrictive on the broad  
invention. Further, it is to be understood that this invention shall not be  
limited to the specific construction and arrangements shown and described  
since various modifications or changes may occur to those of ordinary skill in  
the art without departing from the spirit and scope of the invention as  
25 claimed.

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